IGCSE Revision 3

1. Factorise

(a)
$$2ax + 2ay + 3x + 3y$$
,

$$(x+y)(2a+3)$$

(b)
$$12x^2 + 2x - 30$$
.

$$2(2x-3)(3x+5)$$

2. Complete the square on $x^2 + 3x - 1$. Hence give the vertex of $y = x^2 + 3x - 1$.

$$y = (x + \frac{3}{2})^2 - \frac{13}{4}$$
, Vertex = $(-\frac{3}{2}, -\frac{13}{4})$

3. Find the x^3 coefficient in the expansion of $(2x^2+3x+1)(x^4+3x^3-2x^2+x-3)$.

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- 4. A cuboidal box of cereal has volume 420ml. A sticker talking about the benefits of the cereal has area 40cm². A new, mathematically similar, larger box of cereal is introduced with volume 725.76ml. What would the area of the new sticker be?

 [57.6]
- 5. A cuboidal box of cereal has volume v. A sticker talking about the benefits of the cereal has area a. A new, mathematically similar, larger box of cereal is introduced with volume V. What would the area A of the new sticker be? $a \left(\frac{V}{v} \right)^{\frac{2}{3}}$
- 6. Simplify fully $\frac{8x^2 18}{6x + 9}$.
- 7. Two shapes are mathematically similar. The base on the smaller one is 3.2cm. If the surface area of the larger one is 84cm^2 and the surface area of the smaller one is 21cm^2 .

 What is the length of the base on the larger one?

If the volume of the larger one is V, find an expression for the volume of the smaller one.

 $\frac{V}{8}$

8. For the following, find $\frac{dy}{dx}$:

(a)
$$y = 3x^4 - 2\sqrt{x}$$
.

$$\frac{dy}{dx} = 12x^3 - x^{-\frac{1}{2}}$$

(b)
$$y = \frac{1}{x} - \frac{3}{x^2} + \frac{7x}{3x^7}$$
.

$$\frac{dy}{dx} = -x^{-2} + 6x^{-3} - 14x^{-7}$$

(c)
$$y = \frac{1 - \sqrt{x}}{x}$$
.

$$\frac{dy}{dx} = -x^{-2} + \frac{x^{-\frac{3}{2}}}{2}$$

- 9. A closed cylinder of length l and radius r has a hemisphere of radius r glued to one end. Find a simplified expression for
 - (a) its volume,

 $\frac{\pi r^2(3l+2r)}{3}$

(b) its surface area.

 $\pi r(3r+2l)$

- 10. A car is reduced in a sale by 14%. Its sale price is 1357.08 GBP. What was its original price? 1357.08
- 11. I flick a bias coin 5 times. The probability of a head is 0.7. What is the probability of exactly 3 heads from my 5 throws (in any order)?
- 12. Power P is inversely proportional to the square of time t.
 - (a) If P = 10 when t = 2 find and expression for P in terms of t.

 $P = \frac{40}{t^2}$

- (b) Sketch P against t for t > 0.
- (c) Find t when P = 30.

1.1547 (to 5 sig figs)

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